Ant World

An 'Ant' is a cellular automaton which wanders over a grid of cells obeying certain rules.

Langton's original ant had 2 cell values (0 and 1), two directives (L and R) and a single state (A).

A natural extension of this ant (which we shall continue to call Langton's Ant) allows for multiple cell values and 2, 4 or 6 directives – with the condition that the cell values are updated cyclically. In other words, if a cell has a value of 3, it will be updated to value 4 (or 0 if there are only 4 cell values allowed). In this way, all that is needed to specify a Langton Ant is a string of directives. For example, the string LNRL would define an ant with 4 cell values (0, 1, 2 & 3). If this ant landed on a cell with a cell value of 2, it would update it to 3, turn right and move forward one space.

The four direction of a square grid are as follows:

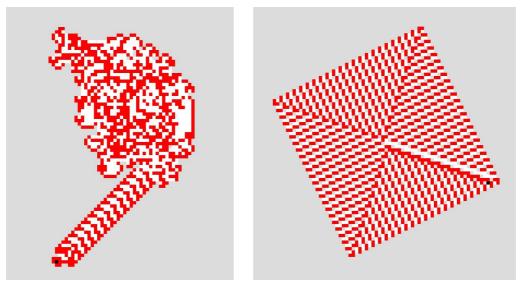
- N No change of heading
- L Turn left 90°
- U Make a U turn
- **R** Turn right 90°

and the six directions on a hexagonal grid are:

- N No change of heading
- L Turn left 60°
- K Turn left 120°
- U Make a U turn
- **Q** Turn right 120°
- R Turn right 120°

Whereas Langton's ants move one step at a time, Linton's ants move a number of steps equal to the current cell value plus one. i.e. if the ant moves onto a cell whose value is 3, it will move in the direction specified 4 steps.

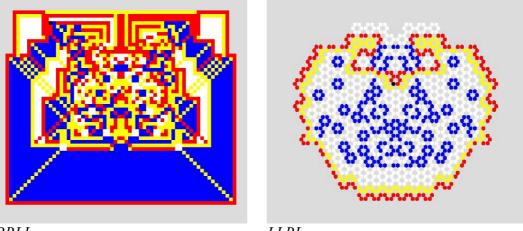
Langton's original ant has the defining string **LR**. After about 10,000 steps or random wanderings it builds a highway down to the SW corner. Linton's ant, with the same defining string does something completely different:



One of the most interesting single state ants is LN which builds a horizontal bar and counts in binary.



If the algorithm consists of pairs of left and right turns, the result is always bilaterally symmetric, Here are a couple of Langton examples using the string **RRLL**:

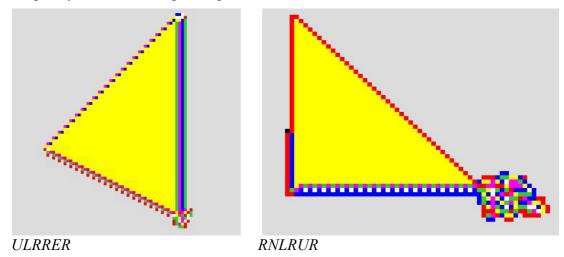


RRLL

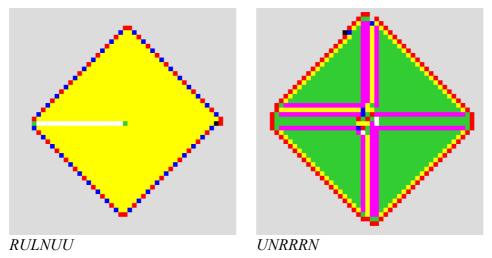
LLRL

All the patterns exhibited here start from an empty grid. Patterns usually only emerge after a short period of chaos. It is perfectly possible that patterns can be 'seeded' with an initial state of cells. For example, it looks as if the ant on the left above could be persuaded to generate a blue red-bordered square with a pair of white diagonals from an appropriate seed.

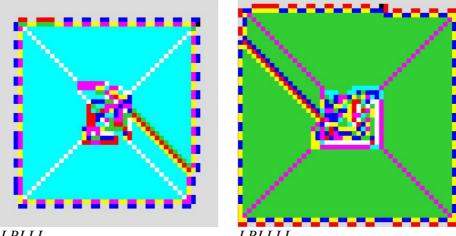
There are many single state ants which build a highway. Many are only 2 cells wide but some can be quite complex. The two ants illustrated below are rather rare. Both are 6-valued ants. Each builds a highway and an ever expanding sail.



One common behaviour is the building of a diamond with one or more diagonals. For example:



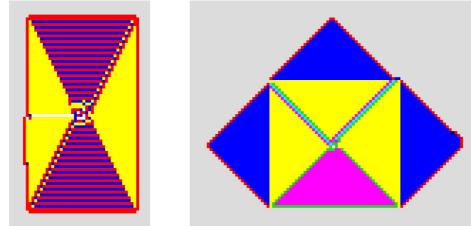
Slightly less common behaviour is the building of a square. For example:



LLRLLL

LRLLLL

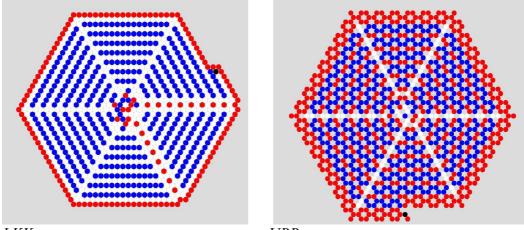
Finally, here are two rather unique examples:



URRR

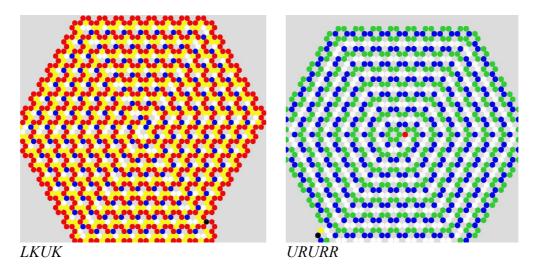
LRNUUNLN

Interesting patterns are more often produced using a hexagonal grid. The most common behaviour is a hexagonal spiral. Here are several examples:

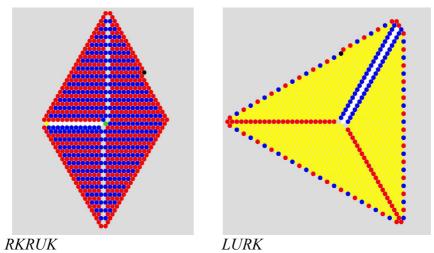




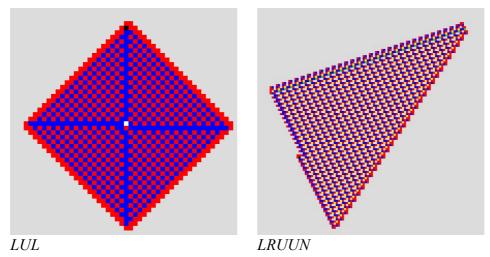




Here are two rather different and unusual patterns.



Here are two patterns generated by Linton's ant.

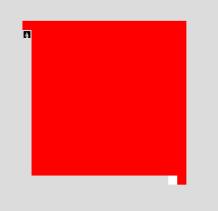


2-state Square Ants

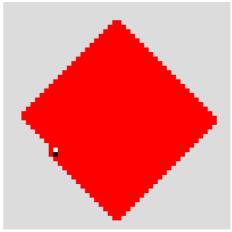
Whereas Langton's and Linton's Ants only have one state, in general an ant may have any number of states. Its behaviour must be specified by a state table which tells what the ant must do given every possible combination of cell values and states. A typical entry is **0RC** which means give the cell the value **0**, turn **R**ight and enter state **C**.

The most interesting ants are those which build regular patterns. In the following examples the captions list first the algorithm used (Langton, Linton, Custom, Busy Beetle), then the kind of board (S2, S4, H2 or H6 where S stands for Square, H for Hexagonal and the number specifies the number of directives). The next two numbers specify the number of states and the number of allowed cell values. Finally the state table is listed in the following order A0, A1, ...; B0, B1, ...; C0, C1, ... etc.

The simplest patterns are a solid square block or a solid diamond:



Custom Ant S2 2 2 1LA 1RB ; OLA 1RA

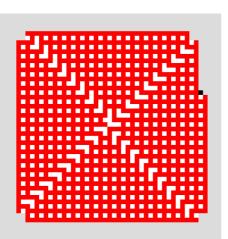


Custom Ant S2 2 2 1LA ORB ; 1LA OLA

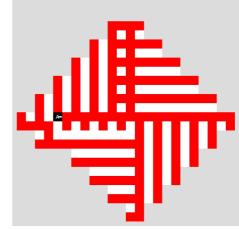
but there are many more interesting designs – e.g.



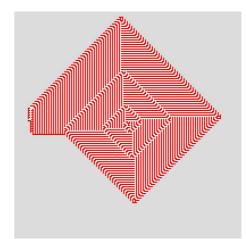
Custom Ant S2 2 2 1LA 0LB ; 0RA 1RB



Custom Ant S2 2 2 0LB 1RA 1RB 0LA

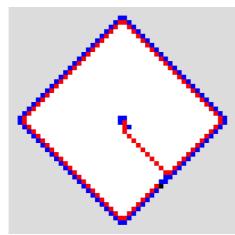


Custom Ant S2 2 2 ORB 1RB ; 1LB 0RA

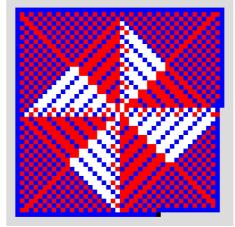


Custom Ant S2 2 2 0LB 0RA 1RB 0LA

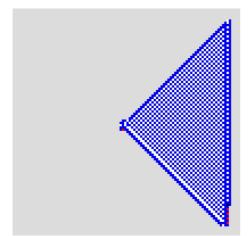
If we allow multiple cell values, the patterns become more colourful but only the octagonal and kite-shaped ones are essentially different .



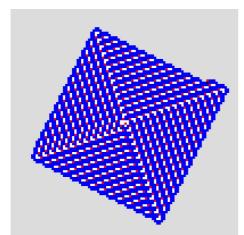
Custom Ant S2 2 3 2LA ORA 1RB ; 2LA ORB 2LA



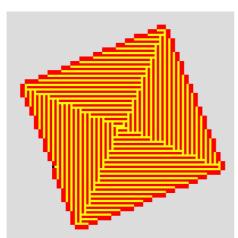
Custom Ant S2 2 3 2LA IRB 2RB ; 2LA 0RB IRA



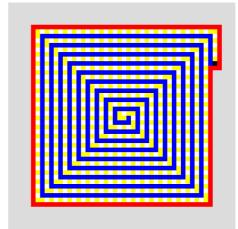
Custom Ant S2 2 3 2RA OLB 1LB ORA ORA 2LA



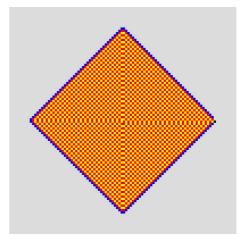
Custom Ant S2 2 4 2RA 0LA 0RB 0RB ; 1RA 0RB 0LB 1RB



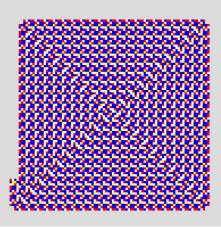
Custom Ant S2 2 4 ORB 3LA 1LA 3LB ; 1LB 1RA ORB 1LB



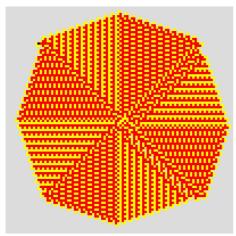
Custom Ant S2 2 4 2RB 0LA 3RA 3LB ; 2LB 3RA 1LB 0RB



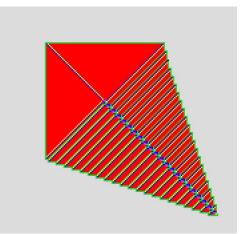
Custom Ant S2 2 4 2LA 1LA 1RB 3LA ; 2LA 2RB 3LA 2RA



Custom Ant S2 2 4 3LA 0RB 2LB 1LA ; 2RA 2RA 2RA 3LA

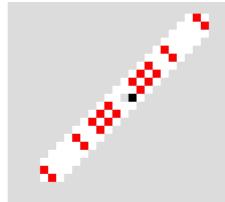


Custom Ant S2 2 4 3LB 3RB 0RB 3LB ; 3RB 1RA 1LB 1RA



Custom Ant S2 2 6 4RB 2RB 4RB 5RA 3LA 4LB ; 4RB 2LA 3RA 5LB 1LB 0LA

If we allow four directives (N, L, U & R) then some new behaviour emerges. One builds a diagonal bar which counts in binary.



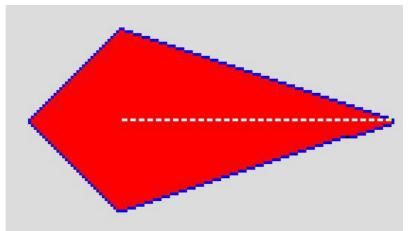
Custom Ant S4 2 2 0LB 1RB ; 1NA 0RA

Another builds a spiral square but not in the way the you might think. It constantly returns to the origin and expands it design from the centre, not the edge!



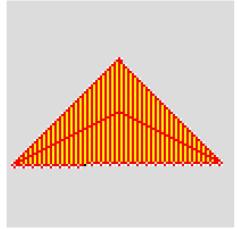
Custom Ant S4 2 2 IRB 0LA ; ILB 0RA

and one which builds a kite:

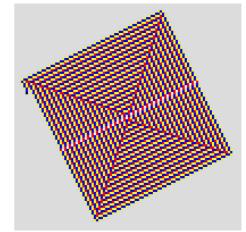


Custom Ant S4 2 4 2RA 1UB 1LA 0LA ; 0NB 3NB 3NA 3RB

These are unusual too:



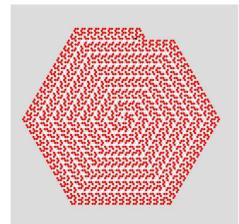
Custom Ant S4 2 4 0LB 3RB 1RA 1RB ; 1NA 1NB 3NB 1UB



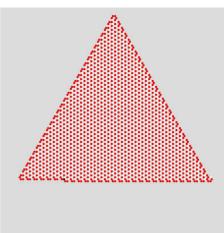
Custom Ant S4 2 4 3LB 1UA 0LB 3UB ; 2NA 0UB 2NB 1LA

2-state Hexagonal Bees

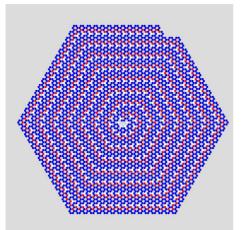
It will not come as a surprise to learn that on a hexagonal grid, most of the patterns generated are either hexagonal or triangular.



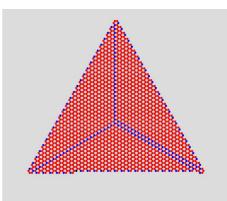
Custom Ant H2 2 2 1RB 1RB ; 1LB 0RA



Custom Ant H2 2 2 0RB 0LB ; 1RB 1LA

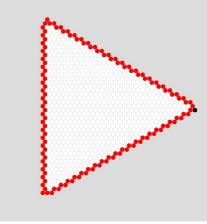


Custom Ant H2 2 3 2LA 2LB 1LB ; ORA 0LB 2RB



Custom Ant H2 2 3 2LB IRA ILA ; ILB 2RA IRA

No essentially new behaviour emerges when we increase the number of cell values or directives but I rather like these two patterns:



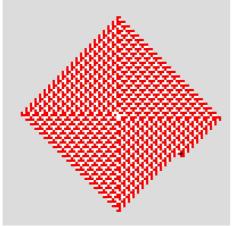
.

Custom Ant H6 2 2 1KB 1NA ; 1NA 0QA

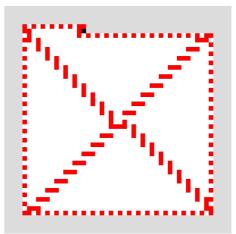
Custom Ant H6 2 3 IRB 0NB 2QB ; 2RB 1QB 0UA

Multiple state Square Ants

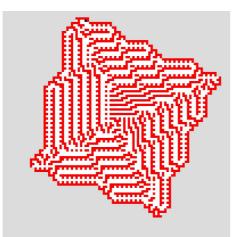
The most common pattern is a square mat. Here are some slightly different designs which I particularly like:



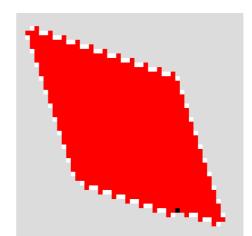
Custom Ant S2 3 2 1LB 0RB ; 0RC 0LA ; 1LC 0RA



Custom Ant S2 3 2 0LB 0RA ; 1LB 0RC ; 0RA 1RB

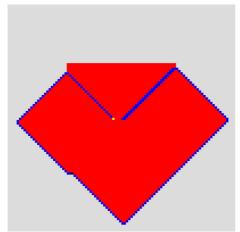


Custom Ant S2 3 2 OLC ORA ; IRB OLA ; IRB ILA

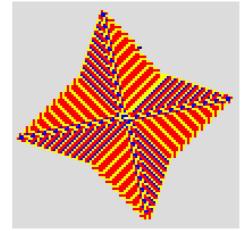


Custom Ant S2 3 2 1LB 1RC ; 0LC 1RC ; 1RA 1RB

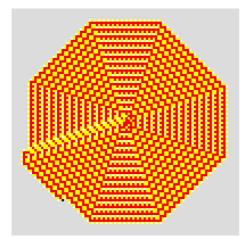
The following patterns were obtained using 4 states, 4 cell values and 2 directives. Each entry in the state table can therefore be one of $4 \times 4 \times 2 = 32$ possibilities. Since there are $4 \times 4 = 16$ entries in the table, the total number of possibilities is 32^{16} which is approximately the same as the number of molecules in a glass of water and vastly exceeds the number of stars on the observable universe. My search program examined over 100,000 random tables in the space of a few hours and selected over 200 patterns that did not either just shoot of to infinity or wander chaotically round the origin. Of these the great majority were either square of diamond mats. The following ones were the most interesting:



Custom Ant S2 4 4 2LB 2RC 2LC 1RA ; 1LB 1RD 2RC 0RA ; 2RD 2RD 3RD 3LD ; 2RC 1RB 1RA 3RC

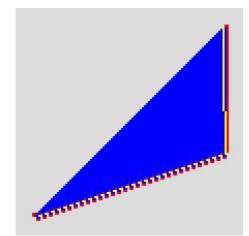


Custom Ant S2 4 4 3RC 2LB 2RA 1RD ; 1RC 3LA 1LC 3LA ; 3RD 1LB 2LB 1LB ; 2LB 0RB 3RA 3LB

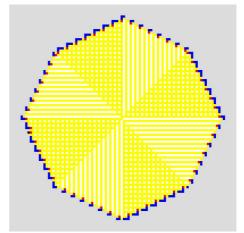


Custom Ant S2 4 4 3RD 3LB 2LA 1RD ; 3RA 3RC 3LB 3RD ; 3LA 2RA 3LC 0RD ; 0RB 3RA 3RB 3LA

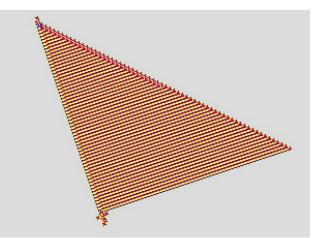
Here are a couple of 'sails':



Custom Ant S2 4 4 1RD 1LA 0LB 2LD ; 1LA 3RA 3LB 2RB ; 0LB 0LA 0LA 0LC ; 1RA 2LD 3RB 1LC

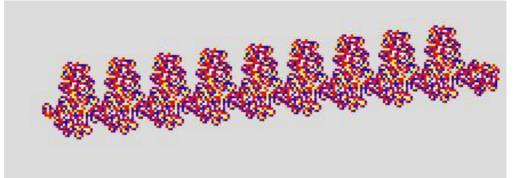


Custom Ant S2 4 4 2LA 2LC 3RC 1RA ; 2LC 0LA 1RB 3RC ; 0RA 0LA 1LC 0LD ; 0LD 3LD 3RD 3LA



Custom Ant S2 4 4 2RB 3LB 0RD 0LD ; 1LC 1LA 3LA 2LC ; 3RA 3RB 0RB 1LC ; 1RB 3RB 3LD 3LB

and this is the most convoluted highway that I have ever seen!



Custom Ant S2 4 4 2LB 2RD 1RA 0RB ; 2RC 3RA 1RB 0LA ; 1RD 0RC 0LD 1RA ; 3LB 1RB 1LA 0RD

Busy Beetles

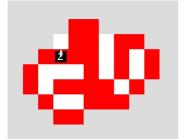
By extension of Turing's concept of a Busy Beaver, I define a Busy Beetle as an Ant with at least one entry with a 'halting state' (\mathbf{Z}). A *Champion* Busy Beetle is defined as the Ant with a given number of cell values, states and directives, which beetles around for the greatest number of steps before halting (or, sometimes, visits the most number of cells before halting).

Values	Longevity	Example State Table
2	5	1LA 0LZ
3	9	1LA 2LA 0LZ
4	25	1LA 2RA3RA 0LZ
5	53	1LA 3RA 4RA 2LA 0LZ
6		

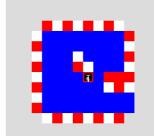
Here is a short table of Champion 1-state Busy Beetles:

cell

The longest lived 2-state Busy Beetles which I have found (with the number of steps and the number of cells visited in brackets) are:

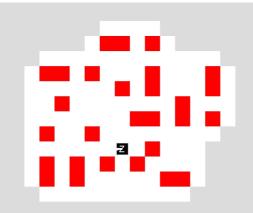


Busy Beetle (121, 41) S2 2 2 1LA 0LB ; 0LZ 1RA



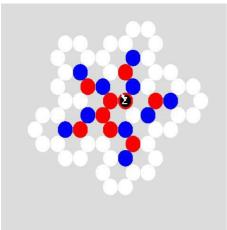
Busy Beetle (485, 96) S2 2 3 2LA 2RA 2LB ; 0LZ 0LB 1LA

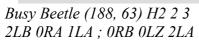
and the longest 3-state Busy Beetles which I have found is:

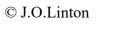


Busy Beetle (878, 137) S2 3 2 1LB 0RA ; 0RC 0LZ ; 0RA 0RB

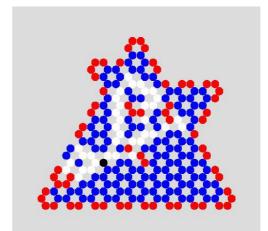
I shall conclude with a few examples of Busy Beetles on a hexagonal grid. (Should we call them Busy Bees?)







Carr Bank, February 2024



Busy Beetle (488, 240) H2 2 3 1LA 2RA 0RB ; 0LZ 0LA 0LA

List of Single State Ants

Algorithm	Square Langton	Hexagonal Langton	Square Linton	Hexagonal Linton
N	Single highway (E)	Single highway (E)	Single highway (E)	Single highway (E)
L	Stable block (4)	Stable ring (6)	Stable block (4)	Stable ring (6)
K		Stable triangle (3)		Stable triangle (3)
U	Stable block (2)	Stable block (2)	Stable block (2)	Stable block (2)
LN	Binary bar	Chaos	Double highway (E)	Chaotic mesh
LL	Square block (4)	Stable ring (6)	Stable block (9)	Stable blob (53)
LK		Chaos		Chaos
LU	Square block (4)	Stable ring (6)	Chaos	Broad highway (NNW)
LQ		Chaotic mesh		Hexagonal mesh
LR	Classic highway	Bilateral doily	Diamond mesh	Hexagonal mesh
KN		Double highway (E)		Double highway (E)
KL		Chaos		Hexagonal mesh
KK		Stable block (3)		Double highway (NNW)
KU		Stable block (3)		Chaotic mesh
KQ		Double highway (SSE)		Hexagonal mat
KR		Chaotic mesh		Hexagonal open mesh
UN	Double highway (E)	Single highway (E)	Single highway (E)	Single highway (E)
UL	Stable block (4)	Stable ring (6)	Diamond mesh	Hexagonal open mesh
UK		Stable triangle (3)		Hexagonal mesh
UU	Stable block (2)	Stable block (2)	Single highway (W)	Single highway (W)
UQ		Stable triangle (3)		Hexagonal mesh
UR	Stable block (4)	Stable ring (6)	Diamond mesh	Hexagonal open mesh
LNN	Ternary bar	Chaos	Double highway (E)	Chaos
LNL	Chaos	Chaos	Double highway (E)	Chaos
LNK		Chaos		Chaos
LNU	Chaos	Chaos	Double highway (E)	Chaos
LNQ		Chaos		Broad highway (NNW)
LNR	Chaos	Chaos	Double highway (E)	Chaos
LLN	Binary bar	Chaos	Chaos	Chaos

LLL	Square block	Hexagonal ring	Triple highway (E)	Quadruple highway (E)
LLK		Chaos		Chaos
LLU	Double highway (E)	Chaos	Diagonal highway (NNE)	Chaos
LLQ		Triangular chaos		Chaos
LLR	Quadruple highway (NW)	Chaos	Chaos	Chaos
LKN		Chaos		Chaos
LKL		Chaos		Broad highway (W)
LKK		Hexagonal spiral		Chaos
LKU		Chaos		Broad highway (W)
LKQ		Chaos		Chaos
LKR		Chaos		Quadruple highway (E)
LUN	Vertical highway	Chaos	Chaos	Chaos
LUL	Horizontal highway	Chaotic mesh	Diamond mat	Hexagonal spiral mesh
LUK		Chaos		Chaos
LUU	Stable block (4)	Stable ring (6)	Chaos	Chaos
LUQ		Chaos		Hexagonal spiral mesh
LUR	Chaos	Chaos	Highway (NE)	Chaos
LQN		Chaos		Chaos
LQL		Hexagonal maze		Chaos
LQK		Chaos		Chaos
LQU		Chaotic rings		Hexagonal spiral mesh
LQQ		Chaos		Chaos
LQR		Chaos		Chaos
LRN	Horizontal highway	Chaos	Chaos	Chaos
LRL	Chaos	Hexagonal mesh	Broad highway (NNE)	Chaos
LRK		Chaos		Chaos
LRU	Stable block (10)	Stable block (24)	Diamond mesh	Chaos
LRQ		Chaos		Chaos
LRR	Chaos	Hexagonal mesh	Chaos	Chaos
KNN		Chaos		Double highway (E)
KNL		Chaos		Double highway (E)
KNK		Double highway		Double highway (E)

KNU	 Chaos	 Double highway (E)
KNQ	 Chaos	 Double highway (E)
KNR	 Chaos	 Double highway (E)
KLN	 Chaos	 Chaos
KLL	 Diagonal highway	 Chaos
KLK	 Chaos	 Chaos
KLU	 Chaos	 Chaos
KLQ	 Chaos	 Hexagonal mesh
KLR	 Chaos	 Chaos
KKN	 Horizontal highway	 Double highway (E)
KKL	 Chaos	 Double highway (NNW)
KKK	 Stable block (3)	 Double highway (NNW)
KKU	 Stable block (7)	 Double highway (NNW)
KKQ	Diagonal highway	Double highway (NNW)
KKR	 Hexagonal mesh	 Double highway (NNW)
KUN	 Horizontal highway	 Chaos
KUL	 Chaos	 Broad highway (SSSW)
KUK	 Stable block (7)	 Hexagonal mesh
KUU	 Stable block (3)	 Chaos
KUQ	 Diagonal highway	 Chaos
KUR	 Chaos	 Chaos
KQN	 Chaos	 Quadruple highway (W)
KQL	 Chaos	 Chaos
KQK	 Diagonal highway	 Chaos
KQU	 Stable block (6)	 Chaos
KQQ	 Diagonal highway	 Broad highway (SE)
KQR	 Chaos	 Chaos
KRN	 Chaos	 Chaos
KRL	 Diagonal highway	 Chaos
KRK	 Chaos	 Chaos
KRU	 Horizontal highway	 Hexagonal open mesh
KRQ	 Chaos	 Chaos

KRR		Chaos		Chaos
UNN	Expanding bar	Expanding bar	Single highway (E)	Single highway (E)
UNL	Chaos	Chaos	Single highway (E) bar	Single highway (E)
UNK		Chaos		Single highway (E)
UNU	Horizontal highway	Horizontal highway	Single highway (E) bar	Single highway (E)
UNQ		Chaos		Single highway (E)
UNR	Chaos	Chaos	Single highway (E) bar	Single highway (E)
ULN	Chaos	Chaos	Triple highway (E)	Chaos
ULL	Horizontal highway	Hexagonal mesh	Triple highway (ENE)	Chaos
ULK		Horizontal highway		Chaos
ULU	Stable block (4)	Stable block (6)	Chaos	Chaos
ULQ		Chaos		Chaos
ULR	Stable block (10)	Stable block (24)	Chaos	Chaos
UKN		Chaos		Triple highway (E)
UKL		Horizontal highway		Chaos
UKK		Chaos		Chaos
UKU		Stable block (3)		Chaos
UKQ		Stable block (6)		Hexagonal mesh
UKR		Chaos		Chaos
UUN	Horizontal highway	Horizontal highway	Single highway (W)	Single highway (W)
UUL	Stable block (4)	Stable block (6)	Single highway (W)	Single highway (W)
UUK		Stable block (3)		Single highway (W)
UUU	Horizontal highway	Horizontal highway	Single highway (W)	Single highway (W)
UUQ		Stable block (3)		Single highway (W)
UUR	Stable block (4)	Stable block (6)	Single highway (W)	Single highway (W)